With the ever-decreasing size of microelectronic devices, growing applications of superlattices, and development of nanotechnology, thermal resistances of interfaces are becoming increasingly central to thermal management. Although there has been much success in understanding thermal boundary conductance at low temperatures, the current models applied at temperatures more common in device operation are not adequate due to our current limited understanding of phonon transport channels. In this study, the scattering processes in Al and Pt films on Al₂O₃ substrates are examined by transient thermoreflectance testing at high temperatures. At high temperatures, traditional models predict the thermal boundary conductance to be relatively constant in these systems due to assumptions about phonon elastic scattering. Experiments, however, show an increase in the conductance indicating potential inelastic phonon processes.

Keywords diffuse mismatch model · Elastic scattering · Inelastic scattering · Phonon · Phonon radiation limit · Thermal boundary conductance

1 Introduction

As electronic products become faster and incorporate greater functionality, they are shrinking in size and mass. The continued trend of miniaturization in micro- and opto-
electronic systems has made the issue of thermal management critical in device design and production. As the length scales continue to decrease, heat transport around active regions in these devices is enhanced/restricted by interfaces between materials and the structures surrounding them. Therefore, accurate predictions of the thermal processes in these devices become dependent on the transport of heat from the device into the packaging material: the thermal boundary conductance across the device/packaging interface [1]. This thermal boundary conductance \( h_{BD} \) is a controlling factor for thermal management in thermoelectrics [2,3], thin-film high-temperature superconductors [4,5], vertical cavity surface emitting lasers [6], and optical data storage media [7].

An understanding of the basic transport mechanisms involved in thermal boundary conductance is critical to the design and engineering of these devices. The main channel for interfacial thermal transport in the majority of these devices is phonon scattering between two materials. The thermal boundary conductance from phonon scattering can be modeled with the diffuse mismatch model (DMM) or the phonon radiation limit (PRL) [8,9]. The DMM uses information about the distribution of the phonon density of states to calculate the incident phonon flux on the interface; the transmission of the phonon flux is calculated from a combination of the acoustic phonon velocities on either side of the interface. To apply the DMM, the assumption of phonon elastic scattering must be made—i.e., a phonon from side 1 with frequency \( \omega \) can only scatter with a phonon from side 2 with the same frequency \( \omega \). Due to this, \( h_{BD} \) is predicted to be constant at temperatures near and above the lower Debye temperature of the two materials comprising the interface since the Debye temperature, \( \theta_D \), is proportional to the phonon cutoff frequency. Similar assumptions are made in the PRL. The PRL calculates the upper limit of \( h_{BD} \) assuming a transmission probability of unity for all phonons that are elastically scattered. These models have been demonstrated to provide good estimates for \( h_{BD} \) at low temperatures \( (T < 50\,\text{K}) \), but at temperatures closer to device operation temperatures, these models do not accurately predict the interfacial thermal processes [10].

In 1993, Stoner and Maris reported \( h_{BD} \) values for a range of acoustically mismatched interfaces over a temperature range from 50 to 300 K [11,12]. As expected from DMM theory, the measured \( h_{BD} \) decreased with sample mismatch, and in each sample, \( h_{BD} \) decreased with temperature. In the sample with the greatest mismatch, Pb/diamond, a value of \( h_{BD} \) was measured that exceeded the DMM prediction by two orders of magnitude. The measured \( h_{BD} \) remained fairly constant, however, over the temperature range, which does not agree with the \( T^3 \) trend predicted by the DMM at low temperatures. This measurement also significantly exceeded the prediction of the PRL. One possible explanation offered for this relatively large \( h_{BD} \) was the occurrence of inelastic scattering—i.e., one or more phonons of frequency \( \omega_1 \) were scattering with one or more phonons of frequency \( \omega_2 \)—thereby offering more channels for transport than the DMM accounts for, leading to an underestimate of \( h_{BD} \) by the DMM. In this particular case, high-frequency diamond phonons could break down into several low-frequency phonons and scatter with the low-frequency phonons in Pb.

Recently, Chen et al. [13] used molecular dynamics simulations to show a linear increase in \( h_{BD} \) across a Kr/Ar nanowire with an increase in temperature from 35 to 55 K. They ascribed this temperature dependence to anharmonic processes. Stevens
From top to bottom, the longitudinal phonon velocity [8] the transverse phonon velocity [8] the atomic number density [25] and the Debye temperature [18,26] are important parameters used in DMM and PRL analysis. The lattice specific heat [25] and thermal conductivity [25] are used in fitting the thermal model [10] to the experimental data to determine $h_{BD}$

e et al. [14] observed thermal transport across the interface of two fcc lattice systems with varying degrees of mass and lattice mismatch using molecular dynamics simulations. A linear increase in $h_{BD}$ was observed at temperatures far above the Debye temperatures of the two materials ($T \gg \theta_D$), and the conclusion of inelastic scattering among the phonons in these systems was verified with a detailed wave packet analysis [15]. This linear increase in $h_{BD}$ at $T \gg \theta_D$ was also recently shown experimentally by Lyeo and Cahill [16]. They observed $h_{BD}$ over a temperature range of 80–300 K on carefully prepared Pb and Bi thin films on diamond substrates with a pump-probe thermoreflectance technique. Like Stoner and Maris, Lyeo and Cahill observed $h_{BD}$ magnitudes higher than the PRL but with a linear increase with temperature, thus agreeing with the aforementioned simulation results.

The purpose of this experimental study is to examine the effects that temperatures around and above $\theta_D$ have on $h_{BD}$. This research examines the assumption of phonon elastic scattering by measuring $h_{BD}$ at interfaces with increased temperature ($T > T_{room}$). The trends in $h_{BD}$ predicted by both the DMM and PRL are compared to experimental data from Al and Pt films on Al$_2$O$_3$ substrates over a temperature range of 300–500 K using the transient thermoreflectance (TTR) technique. By increasing the temperature around and above the Debye temperatures of the metals in these samples, the entire phonon populations of the films are excited. Assuming elastic scattering, a continued increase in temperature should not significantly affect $h_{BD}$ because all of the phonons in the films are already scattering with the lower-frequency phonons in the substrate. However, results indicate a continued increase in $h_{BD}$ above the film $\theta_D$ indicating that higher-frequency substrate phonons activated at the increased temperatures could be scattering with the lower-frequency phonons in the film.

### 2 Models for Thermal Boundary Conductance

The DMM provides a quick and simple calculation of $h_{BD}$ for an interface between two materials. To apply the DMM in its simplest form, the following assumptions must

### Table 1  Thermophysical material properties

<table>
<thead>
<tr>
<th>Material</th>
<th>$\nu_L$ (m·s$^{-1}$)</th>
<th>$\nu_T$ (m·s$^{-1}$)</th>
<th>$n$ (m$^{-3}$)</th>
<th>$\theta_D$ (K)</th>
<th>$C_1 (T = 300 K)$ (J·m$^{-3}$·K$^{-1}$)</th>
<th>$k (T = 300 K)$ (W·m$^{-1}$·K$^{-1}$)</th>
<th>$C_1 (T = 400 K)$ (J·m$^{-3}$·K$^{-1}$)</th>
<th>$k (T = 400 K)$ (W·m$^{-1}$·K$^{-1}$)</th>
<th>$C_1 (T = 500 K)$ (J·m$^{-3}$·K$^{-1}$)</th>
<th>$k (T = 500 K)$ (W·m$^{-1}$·K$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pt</td>
<td>4174</td>
<td>1750</td>
<td>$1.1 \times 10^5$</td>
<td>240</td>
<td>$2.83 \times 10^6$</td>
<td>46</td>
<td>$2.89 \times 10^6$</td>
<td>32.4</td>
<td>$2.95 \times 10^6$</td>
<td>25.6</td>
</tr>
<tr>
<td>Al</td>
<td>6240</td>
<td>3040</td>
<td>$1.0 \times 10^5$</td>
<td>428</td>
<td>$2.34 \times 10^6$</td>
<td>46</td>
<td>$2.5 \times 10^6$</td>
<td>32.4</td>
<td>$2.67 \times 10^6$</td>
<td>25.6</td>
</tr>
<tr>
<td>Al$_2$O$_3$</td>
<td>10890</td>
<td>6040</td>
<td>$3.9 \times 10^4$</td>
<td>1035</td>
<td>$3.0 \times 10^6$</td>
<td>46</td>
<td>$3.64 \times 10^6$</td>
<td>32.4</td>
<td>$4.04 \times 10^6$</td>
<td>25.6</td>
</tr>
</tbody>
</table>
be made [17]: (a) phonons are elastically scattered—i.e., a phonon from side 1 with frequency \( \omega \) can only scatter with a phonon from side 2 with the same frequency \( \omega \); (b) phonon scattering is completely diffuse—i.e., a scattered phonon has no memory of the mode (longitudinal or transverse) or direction of the incident phonon; and (c) the materials on both sides of the interface are elastically isotropic—i.e., the longitudinal and transverse acoustic velocities are constant in all crystallographic directions.

Assuming a small temperature drop across the interface, the principle of detailed balance can be invoked to calculate \( h_{BD} \) [8], the thermal boundary conductance per unit area is given as:

\[
\alpha_{1}(\omega) = \frac{\sum_{j} v_{2,j} \frac{\omega^{2}}{2\pi^{2}v_{2,j}^{3}}}{} + \frac{\sum_{j} v_{1,j} \frac{\omega^{2}}{2\pi^{2}v_{1,j}^{3}}}{\sum_{j} v_{2,j}^{2} + \sum_{j} v_{1,j}^{2}} = \alpha_{1}
\]

It is apparent in Eq. 2 that the transmission probability is independent of frequency, which has been verified by molecular dynamics simulations [19]. In fact, the transmission probability is only dependent on the acoustic velocities of the materials on either side of the interface. Substituting Eq. 2 into Eq. 1, \( h_{BD} \) as a function of temperature can be calculated. The results of these calculations for Al/Al\(_{2}\)O\(_{3}\) and Pt/Al\(_{2}\)O\(_{3}\) systems are shown in Fig. 1. The parameters used in these calculations are summarized in Table 1. Notice that the DMM predicts a constant value of \( h_{BD} \) with temperatures above \( \theta_{D} \) in each material.
The results of the PRL for Al/Al$_2$O$_3$ and Pt/Al$_2$O$_3$ are shown in Fig. 1 with parameters listed in Table 1. Since the PRL represents the upper limit of the elastic contribution to thermal transport, it will always predict a higher $h_{BD}$ than the DMM. Notice that, like the DMM, the PRL predicts a constant $h_{BD}$ at high temperatures ($T \sim \theta_D$). The insets of Fig. 1 show a close-up of the DMM and PRL calculations for the two materials systems in the temperature range of interest in this study.
3 Experimental Considerations

3.1 Samples

Since the goal of this study is to examine any deviations of $h_{BD}$ from the DMM and PRL elastic scattering assumptions at high temperatures, material systems were chosen to encompass different regimes in which the amount of temperature dependence in $h_{BD}$, as predicted by DMM, would vary. The Pt/Al$_2$O$_3$ and Al/Al$_2$O$_3$ material systems allow investigation of $h_{BD}$ at temperatures around $\theta_D$ of Al and well above $\theta_D$ of Pt. Assuming elastic scattering, an increase in $h_{BD}$ is expected in Al over the temperature range since the phonon population will increase until $T > \theta_D$. However, in Pt where $\theta_D < T_{room}$ an increase in $h_{BD}$ should not occur since the entire phonon population is excited. Any increase when $T > \theta_D$ could be evidence of a high-frequency substrate phonon exciting from the elevated temperature and scattering with two or more lower-frequency film phonons.

The Al and Pt film thicknesses were 75 and 50 nm, respectively, chosen to be $\sim$50% greater than the electron mean free path in these metals to minimize electron scattering at the boundary since the interest in this study is interfacial phonon transport [20]. These thicknesses were also necessary to ensure that it was possible to extract viable $h_{BD}$ information from the TTR data [10]. The Al and Pt films were deposited on factory polished Al$_2$O$_3$. The depositions took place in a multisource, high vacuum thin film sputter deposition system, a Supersystem III manufactured by the Kurt J. Lesker Company capable of pumping down to $10^{-7}$ Torr. All substrates were (ETM) spin cleaned with reagent alcohol (90.7% ethyl alcohol; 4.8% isopropyl alcohol; 4.5% methyl alcohol; 0.12% water), trichloroethylene, and methanol, then subsequently baked for 5 min at 400 K to remove any residual water that may have formed at the substrate surface as a result of the spin clean. The substrates were subjected to a 5 min, 100 W backsputter etch prior to film deposition to remove the oxide layer and any additional contaminants.

3.2 Experimental Setup

The TTR data were taken with a pump-probe experimental setup where the primary output of the laser system emanates from a Coherent RegA 9000 amplifier operating at a 250 kHz repetition rate with about 4 $\mu$J per pulse and a 150 fs pulse width at 800 nm. The pulses were split at a 9:1 pump to probe ratio. The pump beam, modulated at 125 kHz, was focused down to a 100 $\mu$m radius spot size to achieve 10 J·m$^{-2}$ fluence. The probe beam was focused to the middle of the pump beam to achieve a pump-to-probe fluence ratio of 10:1. The radii of the pump and probe beams were measured with a sweeping knife edge [21]. Although the low repetition rate of the RegA system and the “one shot on—one shot off” modulation rate of the pump beam ensures minimal residual heating between pump pulses, the phase of the signal must still be taken into account. The phase correction was performed by the procedures for signal phase adjustment outlined in the references [21].
For long scans, alignment of the pump and probe spots can become an issue [10, 21, 22]. To avoid misalignment problems, the probe beam was collimated before the probe delay stage and profiled with a sweeping knife-edge at all time delays. In this study, a pump to probe radius ratio of 10:1 was used, and the probe was aligned with the delay stage resulting in less than 1.5 and 4.0 µm drift along the horizontal and vertical axes perpendicular to the surface, respectively. These spot characteristics result in less than 1% error due to misalignment of the beams [21].

The samples were mounted to a 5 mm thick Al plate attached to a Minco 5419 silicon rubber resistive heater. The samples were mounted on the front of the Al plate with Molykote 44 high-temperature vacuum grease, and the sides and back of the aluminum plate/heater were insulated with high-temperature millboard insulation. Thermocouple holes were drilled 1 mm underneath the front surface of the Al plate in four locations surrounding the sample to monitor the temperature of the sample. For each desired temperature, the Al block was heated and held at constant temperature for ~2 h to ensure that the sample/Al block system equilibrated before TTR measurements were taken. After several measurements at a certain temperature, the heater was turned off and the temperature dropped to room temperature. Room-temperature measurements were again taken after the system returned to room conditions, and these measurements were compared to ensure that the sample was not damaged as a result of the heating. The value of $h_{BD}$ was determined by fitting the TTR data to the thermal model discussed in detail in Stevens et al. [10]. Repeatable results were found at all temperatures. The data presented in this article are the statistical averages of the data at each temperature, and a deviation of less than 10% from the mean was calculated.

4 Results

The TTR data are plotted against temperature for the Al and Pt material systems in Figs. 2 and 3, along with the calculations for the DMM and PRL in these systems. The line fit to the data depicts the linearity of the relationship between temperature and $h_{BD}$ observed in the experiments. The slope of this line, $\eta$, is also presented in these figures along with the Debye temperatures of the materials. Figure 2 shows the measured $h_{BD}$ across the Al/Al$_2$O$_3$ interface. In addition to data measured in this study (300 K < $T$ < 500 K), low-temperature data from Stoner and Maris [12] are included. The linear fit included the data from this study and Stoner and Maris data from 150 K to room temperature. At 150 K, $h_{BD}$ appears to lose its $T^3$ dependence. Over the temperature range in this study, the experimental data increases by almost 100%, where the DMM, which would consider only elastic scattering, only predicts a 10% increase. In addition, the data above $\theta_D$ of Al increase 25% over a 50 K temperature increase. The linear increase above $\theta_D$ of Al suggests that inelastic phonon processes may occur between a single high-frequency phonon in the Al$_2$O$_3$ and two or more lower-frequency phonons in Al. As the temperature is driven above $\theta_D$ of Al, the entire phonon population in Al is excited. However, the linear increase of Al$_2$O$_3$ phonon population continues and, therefore, the increase in $h_{BD}$ above the $\theta_D$ of Al could be evidence of inelastic scattering. The continued linear trend observed from the data from Stoner and Maris to the high-temperature data even above $\theta_D$ of Al,
indicates that there is a smooth transition between regimes where $h_{BD}$ is dominated by elastic and inelastic scattering.

To examine the regime where inelastic scattering would dominate (i.e., temperatures above the Debye temperature of only one of the materials, so that the entire phonon population of one material is excited but not the other), the highly mismatched Pt/Al$_2$O$_3$ system was studied. Lyeo and Cahill [16] found this regime at low temperatures with Pb and Bi on diamond. The Al/Al$_2$O$_3$ system gives hints towards anharmonic processes with the data 50 K above $\theta_D$. However, due to the less than room temperature $\theta_D$ of Pt, the highly mismatched Pt/Al$_2$O$_3$ shows promising data that further support the findings of inelastic scattering processes in high-temperature regimes. Figure 3 shows $h_{BD}$ versus temperature TTR results. The temperature of this interface was increased to over twice $\theta_D$ of Pt. Over the investigated temperature range, $h_{BD}$ increases by over 50%, which is a similar result to previous calculations that model elastic and inelastic scattering [14]. The DMM and PRL predict an increase in $h_{BD}$ of less than 5% over this temperature range. Since the change in the Pt phonon population is constant above $\theta_D$ of Pt, the linear increase in $h_{BD}$ observed in the TTR data indicates that inelastic phonon processes are occurring.
Fig. 3 Measured thermal boundary conductance across the Pt/Al₂O₃ boundary. Change in $h_{BD}$ at these high temperatures ($T \gg \theta_D$, Pt) is linear where the change in $h_{BD}$ predicted from the DMM and PRL assuming only elastic collisions contributing to transport is relatively flat.

The experimental data in this study are compared to the DMM and PRL models which were calculated assuming a Debye density of states. The Debye density of states provides a quick and simple calculation of the DMM and PRL; however, several studies have showed that using a more realistic density of states could significantly change the resulting calculations [19,23,24]. Recent calculations by Reddy et al. [23] of metal films on semiconductor substrates use the Born von-Karman approximation (BKM) to calculate an exact phonon dispersion in the DMM. The trend in the models resulting from these calculations (i.e., change in $h_{BD}$ with temperature which becomes negligible at temperatures approaching $\theta_D$) changes with the BKM calculation [23]. With this more realistic density of states, the change in $h_{BD}$ with temperature becomes negligible at much lower temperatures. Applying this conceptual shift to the DMM and PRL data results in an even more drastic difference between the trends in the experimental data and the trends in the models assuming only elastic phonon collisions presented in Figs. 2 and 3. This gives further evidence that inelastic scattering events are participating in $h_{BD}$ at higher temperatures.

Comparing the slopes of $h_{BD}$ versus temperature of the Al/Al₂O₃ and Pt/Al₂O₃ samples gives interesting insight into the contributions of the elastic and inelastic processes. The slope of the data on Pt/Al₂O₃, which is taken at temperatures well above $\theta_D$, Pt, is $\eta = 2.2 \times 10^5$ W·m⁻²·K⁻² calculated from the best fit line estimate to the data. However, for the Al/Al₂O₃ sample, $\eta = 6.5 \times 10^5$ W·m⁻²·K⁻², nearly three
times greater than that of the Pt/Al2O3 sample. Over the temperature range of the data for Al/Al2O3 presented in Fig. 2, the increase in $h_{BD}$ can be attributed to both elastic and inelastic scattering. In the event of inelastic scattering, a high-frequency Al2O3 phonon does not need to break down into many low-frequency phonons for energy transmission. However, over the temperature range of the data for Pt/Al2O3 presented in Fig. 3, for reasons previously discussed, the continued increase can be ascribed to inelastic scattering. Due to the low Debye temperature of Pt, an Al2O3 phonon would have to break down several times for energy transmission (more times than for energy transmission from Al). This large phonon decomposition cascade could reduce energy transmission, therefore partly causing $\eta$ for the Pt/Al2O3 sample to be less than $\eta$ for the Al/Al2O3 sample. Contributions of elastic scattering in the measured $h_{BD}$ on the Al/Al2O3 sample could also add to this difference in $\eta$.

5 Conclusions

Thermal management in micro- and opto-electronic devices is becoming critical to further development. The mechanisms of interfacial phonon transport must be fully understood to accurately predict thermal processes in these devices. Although traditional models predict thermal boundary conductance at low temperatures ($T \ll T_{room}$) relatively well, at temperatures closer to device operating temperatures these models fail to account for inelastic phonon scattering processes which could contribute to interface conductance. To test the effect of these inelastic processes, TTR experiments were performed on Al and Pt films on Al2O3 substrates at elevated temperature ($T > T_{room}$). At these temperatures, the thermal boundary conductance is assumed to be relatively constant by traditional models considering only elastic scattering. At temperatures around and above the Debye temperature of the metal film, the thermal boundary conductance was shown to increase linearly with temperature indicating that inelastic scattering is contributing to interfacial transport.

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References

9. N.S. Snyder, Cryogenics 10, 89 (1970)
11. The term "acoustic mismatch" describes two materials that have significantly different acoustic velocities; the degree of the acoustic mismatch can be easily determined by comparing the materials’ Debye temperatures, $\theta_D$.